Q1. True or False? Explain your reasoning. If the zero vector is part of a set of vectors, then that set is linearly dependent.

It’s true. To assume that v is a vector space and consider **{0, v1 ,v2 , … ,vn } vi∈v.** To examine **c0\*0 + c1\*v1 + c2\*v2 +…+ cn\*vn = 0**. Let **c0 = 1** and **c1 = c2 = c3 … cn = 0**. So the equation can be expressed as **1\*0 + 0 \* v1 + 0 \*v2 + 0 \* v3 + … +0 \* vn = 0**. It shows that there exists **ci’**s not all zero and still satisfy the equation.

Q2. True or False? Explain your reasoning. If a set of vectors is linearly dependent so is any larger set which contain it.

It’s true. To assume that **p** is a vector space and consider **{p1, p2, p3, …, pn} pi ∈p** is dependent. And there are coefficients **a1, a2, … an,** are not all zero. The equation can be expressed as

**a1p1 + a2p2 + … + anpn = 0**

Now let **q** is **p’s** larger set and **m>= n**, and consider { **p1, p2, p3, …, pn** ,**pn+1, pn+2, … , pm**}. The equation of **q** can be expressed as

**b1p1 + b2p2 + … + bnpn + bn+1pn+1 + bn+2pn+2 + … + bmpm = 0**

Take **b1 = a1, b2 = a2, … ,bn = an**, and **bn+1 = bn+2 = … = bm = 0**. Because **ai’**s are not all zero, **bi**’sare not all zero either. We got the equations

**b1p1 + b2p2 + … + bmpm = a1p1 + a2p2 + … + anpn = 0**

So { **p1, p2, …, pm**} is linearly dependent as well.